

Name

Class



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# Direct/inverse proportion

(9 – 1) Topic booklet

## Higher

These questions have been collated from previous years GCSE Mathematics papers.

**You must have:** Ruler graduated in centimetres and millimetres, protractor, pair of compasses, pen, HB pencil, eraser.

Total Marks

### Instructions

- Use **black** ink or ball-point pen.
- **Fill in the boxes** at the top of this page with your name, centre number and candidate number.
- Answer **all** questions.
- Answer the questions in the spaces provided
  - *there may be more space than you need.*
- Diagrams are NOT accurately drawn, unless otherwise indicated.
- You must **show all your working out**.
- If the question is a **1H** question you are not allowed to use a calculator.
- If the question is a **2H** or a **3H** question, you may use a calculator to help you answer.

### Information

- The marks for **each** question are shown in brackets
  - *use this as a guide as to how much time to spend on each question.*

### Advice

- Read each question carefully before you start to answer it.
- Keep an eye on the time.
- Try to answer every question.
- Check your answers if you have time at the end.

**Answer ALL questions  
Write your answers in the space provided.  
You must write down all the stages in your working.**



**6** A company orders a large number of plates from a factory.

It would take 30 hours to make all the plates using 4 machines.

How many machines are needed to make all the plates in 6 hours?

6 At a depth of  $x$  metres, the temperature of the water in an ocean is  $T$  °C.  
At depths below 900 metres,  $T$  is inversely proportional to  $x$ .



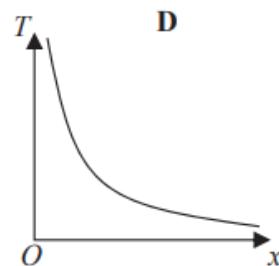
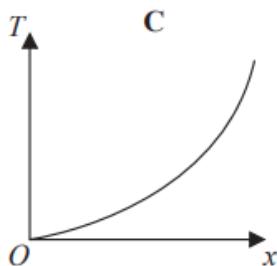
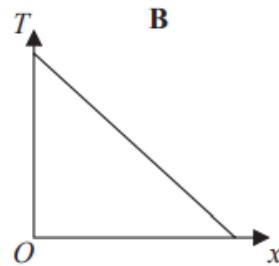
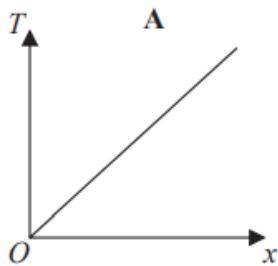
$T$  is given by

$$T = \frac{4500}{x}$$

(a) Work out the difference in the temperature of the water at a depth of 1200 metres and the temperature of the water at a depth of 2500 metres.

..... °C  
(3)

Here are four graphs.



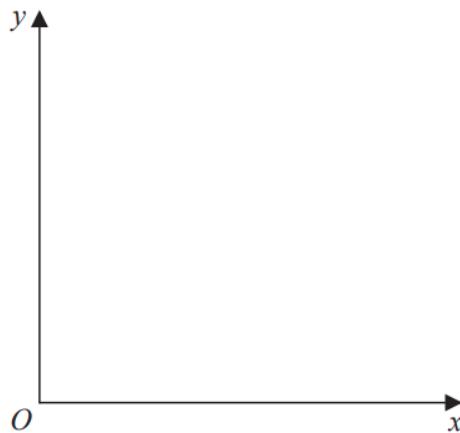
One of the graphs could show that  $T$  is inversely proportional to  $x$ .

(b) Write down the letter of this graph.

.....  
(1)

8 (a) Using the axes below, sketch a graph to represent the statement

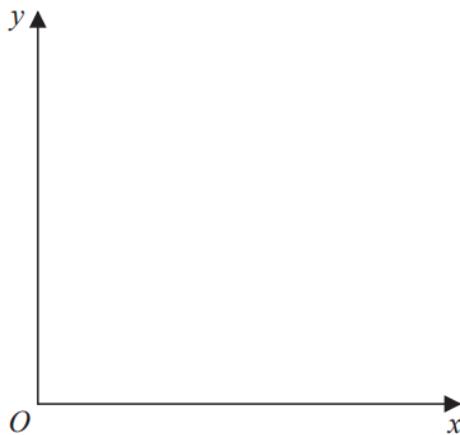
$y$  is directly proportional to  $x$



(1)

(b) Using the axes below, sketch a graph to represent the statement

$y$  is inversely proportional to  $x$



(1)

**10**  $y$  is inversely proportional to  $x$

When  $x = 1.5$ ,  $y = 36$

Find the value of  $y$  when  $x = 6$

Specimen 2 – Paper 1H

**(Total for Question 10 is 3 marks)**

**12**  $f$  is inversely proportional to  $d^2$

$f = 3.5$  when  $d = 8$



(a) Find an equation for  $f$  in terms of  $d$ .

.....  
(2)

(b) Find the positive value of  $d$  when  $f = 10$

Give your answer correct to 3 significant figures.

$d =$  .....  
(2)

June 2024 – Paper 2H

**(Total for Question 12 is 4 marks)**

13  $p$  is inversely proportional to  $t$

Complete the table of values.

$t$	100	25		2
$p$	1		5	

13 The table shows a set of values for  $x$  and  $y$ .

$x$	1	2	3	4
$y$	9	$2\frac{1}{4}$	1	$\frac{9}{16}$

$y$  is inversely proportional to the square of  $x$ .

(a) Find an equation for  $y$  in terms of  $x$ .

(2)

(b) Find the positive value of  $x$  when  $y = 16$

(2)

**13**  $d$  is inversely proportional to  $c$



When  $c = 280$ ,  $d = 25$

Find the value of  $d$  when  $c = 350$

$d = \dots$

Sample 1 – Paper 2H

**(Total for Question 13 is 3 marks)**

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**13**  $y$  is directly proportional to  $x$ .

$y = 24$  when  $x = 1.5$

Work out the value of  $y$  when  $x = 5$

$y = \dots$

June 2023 – Paper 1H

**(Total for Question 13 is 3 marks)**

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**14**  $y$  is proportional to  $x^2$

$$y = 3 \text{ when } x = 0.5$$



$x$  is inversely proportional to  $w$

$$x = 2 \text{ when } w = 0.2$$

Find the value of  $y$  when  $w = 2$

$$y = \dots$$

November 2023 – Paper 2H

**(Total for Question 14 is 5 marks)**

**14**  $y$  is inversely proportional to  $x^3$

$$y = 44 \text{ when } x = a$$



Show that  $y = 5.5$  when  $x = 2a$

November 2018 – Paper 3H

**(Total for Question 14 is 3 marks)**

14  $y$  is inversely proportional to  $d^2$

When  $d = 10$ ,  $y = 4$

$d$  is directly proportional to  $x^2$

When  $x = 2$ ,  $d = 24$

Find a formula for  $y$  in terms of  $x$ .

Give your answer in its simplest form.

14  $D$  is directly proportional to the cube of  $n$ .

Mary says that when  $n$  is doubled, the value of  $D$  is multiplied by 6

Mary is wrong.

Explain why.



Specimen 2 – Paper 2H

**(Total for Question 14 is 1 mark)**

(1)

15 A pendulum of length  $L$  cm has time period  $T$  seconds.



$T$  is directly proportional to the square root of  $L$ .

The length of the pendulum is increased by 40%.

Work out the percentage increase in the time period.

%

Specimen 1 – Paper 2H

**(Total for Question 15 is 3 marks)**

**16**  $y$  is directly proportional to  $\sqrt[3]{x}$

$$y = 1 \frac{1}{6} \text{ when } x = 8$$

Find the value of  $y$  when  $x = 64$

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November 2017 – Paper 1H

**(Total for Question 16 is 3 marks)**

17  $y$  is directly proportional to the square root of  $t$ .

$$y = 15 \text{ when } t = 9$$

$t$  is inversely proportional to the cube of  $x$ .

$$t = 8 \text{ when } x = 2$$

Find a formula for  $y$  in terms of  $x$ .

Give your answer in its simplest form.

17  $x$  is directly proportional to the square of  $y$ .  
 $y$  is directly proportional to the cube of  $z$ .



$z = 2$  when  $x = 32$

Find a formula for  $x$  in terms of  $z$ .

**18**  $x$  is proportional to  $\sqrt{y}$  where  $y > 0$

$y$  is increased by 44%

Work out the percentage increase in  $x$ .

.....%

**20**  $h$  is inversely proportional to  $p$

$p$  is directly proportional to  $\sqrt{t}$

Given that  $h = 10$  and  $t = 144$  when  $p = 6$   
find a formula for  $h$  in terms of  $t$